

# A Dynamic Model for the Energy Management of Microgrid-Enabled Production Systems

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## Abstract

In recent years, industrial facilities are devoting ever greater attention to the importance of energy in their operations. It directly supports the challenges of high availability, quality excellence, and compliance with ever more ambitious sustainability targets. Such objectives are often beyond the scope of local electric utilities, and so this work, instead, considers *microgrid-enabled production systems*. In such a case, the production enterprise is motivated to in-source its energy supply so as to tailor its management and delivery to the needs of its production system. The introduction of microgrids to a production system setting opens several new industrial energy management activities. Here, the microgrid's dynamic power balancing activities in the operations time scale are of greatest importance. The power supply, which may potentially be variable, must be matched to the industrial loads which are a byproduct of production activities. Therefore, this article seeks to develop a Dynamic Energy Management Model for Microgrid-Enabled Production Systems. The model is based on a *hetero-functional graph theory* rooted in the Axiomatic Design for Large Flexible Engineering Systems and timed Petri nets. The static stability of the microgrid is analyzed using power flow analysis. The resulting model is applied to an illustrative example in which a multi-resource production system is coupled to a microgrid with several types of power generation. The outcomes of the example show that the variable electricity demand imposed by production activities is ill accommodated by renewable energy sources alone. Consequently, the stability of the microgrid is maintained by a dispatchable generator. This holistic model, therefore, includes the impact of the production schedule on greenhouse gas emissions.

*Keywords:* Demand Response, Axiomatic Design, petri net model, manufacturing system, smart grid, multi-layer networks

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## Nomenclature

$(\cdot)^V$	Vectorization of a matrix, equivalent to $\text{vec}(\cdot)$	$\epsilon_{xl_i}$	Action or event in the product net of product $l_i$
$\cdot$	Hadamard product	$\Lambda_{\mu i}$	Product transformation feasibility matrix
$\otimes$	Aggregation operator	$\mathbf{0}^{\sigma(n) \times \sigma(m)}$	Zeros matrix of size $\sigma(n) \times \sigma(m)$

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$\mathbf{V}$	Vector of nodal voltage levels	$H$	Set of transporting resources
$\mathbf{Y}$	Bus admittance matrix	$H_{MG}$	The set of Transmission Lines
$\mathbb{1}^n$	column ones vector of predefined length $n$	$H_{PS}$	The set of Material Handlers
$\mathbb{P}$	Projection operator	$i$	Index for DOF $\psi_i$ in set $\mathcal{E}_S$
$\mathbb{P}_H$	Projection matrix	$j$	Index for transformation process $p_{\mu j}$ in set $P_\mu$
$\mathbb{P}_M$	Projection matrix	$J_\varphi$	Holding knowledge base
$\odot$	Matrix boolean multiplication	$J_H$	Transportation knowledge base
$\ominus$	Matrix boolean subtraction	$J_M$	Transformation knowledge base
$\otimes$	Kronecker product	$J_S$	System Knowledge Base
$\Phi$	State transfer function dependent on $Q_B[k]$ and $U[k]$	$J_{\bar{H}_{MG}}$	Microgrid refined transportation knowledge base
$\Phi_T$	State transition function dependent on $Q[k]$ , $U^- [k]$ , and $U^+ [k]$	$J_{\bar{H}_{MPS}}$	Microgrid-Enabled Production System refined transportation knowledge base
$\psi_i$	DOF $i$ in the set of structural degrees of freedom $\mathcal{E}_S$	$J_{\bar{H}_{PS}}$	Production system refined transportation knowledge base
$\sigma()$	The size of the set ()	$J_{\bar{H}}$	Refined transportation knowledge base
$\theta_\psi$	The associated voltage angle relative to a predefined reference bus	$J_{\varphi_{MG}}$	Microgrid holding knowledge base
$\tilde{J}_{MG}$	Microgrid transformation knowledge base unrelated to production	$J_{\varphi_{PS}}$	Production system holding knowledge base
$\tilde{M}_{MG}$	The set of Microgrid generators and loads unrelated to production	$J_{H_{MG}}$	Microgrid transportation knowledge base
$\tilde{P}_{\mu MG}$	The set of microgrid generating and consuming processes unrelated to production	$J_{H_{PS}}$	Production system transportation knowledge base
$\underline{\mathbf{R}}$	Set of aggregated resources	$J_{M_{MG}}$	Microgrid transformation knowledge base
$\underline{r}_a$	Aggregated resource $a$ in set $\underline{\mathbf{R}}$	$J_{M_{MPS}}$	Microgrid-Enabled Production System transformation knowledge base
$a$	Index for aggregated resource $\underline{r}_a$ in set $\underline{\mathbf{R}}$	$J_{M_{PS}}$	Production system refined transformation knowledge base
$A_{i,j}$	Matrix used for the product transformation feasibility matrix	$J_{MG}$	Microgrid Knowledge Base
$B$	Set of independent buffers	$J_{PS}$	Production System Knowledge Base
$B_S$	Set of buffers	$K_S$	System constraints matrix
$B_{MG}$	The set of Substations & Storage	$l_i$	Index for product
$B_{PS}$	The set of Independent Input & Output Buffers	$M$	Set of transforming resources
$B_{S_{PS}}$	The set of Production system buffers	$M_{\mathcal{E}_{\psi H}}^+$	Positive transportation degree of freedom incidence matrix
$b_{sy}$	Buffer $y$ in set $B_S$	$M_{\mathcal{E}_{\psi H}}^-$	Negative transportation degree of freedom incidence matrix
$C_C$	capacity vector of size $\sigma(\mathcal{E}_S) \times 1 \in \mathbb{N}^{\sigma(\mathcal{E}_S)}$	$M_H^+$	Incidence “in” matrix
$d_\psi$	Event duration of action $\psi$	$M_H^-$	Incidence “out” matrix
$DOF_S$	The number of structural degrees of freedom	$M_{MG}$	The set of Generators & Loads
$e_i^n$	$i^{th}$ elementary basis vector of predefined length $n$	$M_{MPS}$	The set of Microgrid-Enabled Production System transformation resources
$e_{wv}$	Action in the SysML sense	$M_{PS}$	The set of Machines
$g$	Index for holding process $p_{\varphi g}$ in set $P_\varphi$	$M_{\mathcal{E}_{\psi H}}$	Transportation degree of freedom incidence matrix
$g_\psi$	Complex power assigned to the structural degree of freedom $\psi$	$P$	Set of system’s processes
		$P_\eta$	Set of transportation processes
		$P_\mu$	Set of transformation processes
		$P_\psi$	The active power injection from ground

$P_\varphi$	Set of holding processes	$U_{l_i}[k]$	Binary product net firing vector corresponding with product $l_i$ at time $k$
$p_w$	System process $w$ in set $P$	$v$	Index for system resource $r_v$ in set $R$
$P_{\bar{\eta}PS}$	The set of Production System refined transportation processes	$v_\psi$	The associated voltage magnitude relative to ground
$P_{\bar{\eta}}$	Refined transportation processes	$W$	Weighting function on arcs
$P_{\eta MG}$	The set of Microgrid Transportation Processes	$w$	Index for system process $p_w$ in set $P$
$P_{\eta PS}$	The set of Production System Transportation Processes	$w_{E\psi}$	The set of algebraic state variables in the microgrid
$p_{\eta u}$	Transportation process $u$ in set $P_\eta$	$W_{l_i}$	Weighting function on product arcs
$p_{\mu j}$	Transformation process $j$ in set $P_\mu$	$y$	Index for Buffer $b_{sy}$ in set $B_S$
$P_{\mu MG}$	The set of Microgrid Transformation Processes	$y_{\psi h}$	An admittance assigned to the transportation structural degree of freedom
$P_{\mu MPS}$	The set of Microgrid-Enabled Production System transformation processes	$y_\psi^*$	An admittance assigned to the structural degree of freedom $\psi$
$P_{\mu PS}$	The set of Production System Transformation Processes	$\mathcal{A}$	Aggregation matrix
$p_{\varphi g}$	Holding process $g$ in set $P_\varphi$	$\mathcal{E}_S$	Set of events, transitions, or structural degrees of freedom
$P_{\varphi MG}$	The set of Microgrid Holding Processes	$\mathcal{E}_{\psi H}$	Power system transportation degrees of freedom
$P_{\varphi PS}$	The set of Production System Holding Processes	$\mathcal{E}_{\psi M}$	Power system transformation degrees of freedom
$P_{MG}$	The set of microgrid processes	$\mathcal{E}_{l_i}$	Set of product events that describe the transformation of the product between product places
$P_{PS}$	The set of production system processes	$\mathcal{M}$	Petri net incidence matrix of size $\sigma(B_S) \times \sigma(\mathcal{E}_S)$
$Q[k]$	Petri net marking vector, $Q[k] = [Q_B[k]; Q_E[k]]$	$\mathcal{M}^+$	Positive (ingoing) Petri net incidence matrix ( $w(e_{wv}, b_y)$ )
$Q_\psi$	The associated reactive power injection from ground	$\mathcal{M}^-$	Negative (outgoing) Petri net incidence matrix ( $w(b_y, e_{wv})$ )
$Q_B[k]$	Marking (or discrete state) vector of size $\sigma(B_S) \times 1$	$\mathcal{M}_E$	Matrix that introduces degrees of freedom in Power Flow Analysis
$Q_E[k]$	Transition state marking vector of size $\sigma(\mathcal{E}_S) \times 1$	$\mathcal{M}_{l_i}$	Product arc relations that describe which products or components receive which product events
$Q_{l_i}[k]$	Marking vector that describes the product's evolution at time step $k$	$\mathcal{M}_{PN}$	Set of arcs from places to transitions and from transitions to places in the Petri net graph.
$R$	Set of system's resources	$\mathcal{M}_{PS}^+$	Positive (ingoing) production system incidence matrix
$r_v$	System resource $v$ in set $R$	$\mathcal{M}_{PS}^-$	Negative (outgoing) production system incidence matrix
$R_{PS}$	The set of Production system resources	$\mathcal{N}_{l_i}$	Product petri net for product $l_i$
$S_{l_i}$	Set of product places for product $l_i$ that represents a product component at a raw, work-in-progress, or final stage of production	$\mathcal{S}$	Marked Petri Net (Graph)
$t_k$	Time at time step $t_k + d_\psi$	$\mathcal{S}$	Scheduled Event List
$t_k$	Time at time step $k$	$\mathcal{U}[k]$	Binary product firing matrix at time step $k$ of size $\sigma(\mathcal{E}_S) \times \sigma(L)$
$u$	Index for transportation process $p_{\eta u}$ in set $P_\eta$	$\mathcal{Y}$	Transportation degree of freedom admittance matrix
$U[k]$	Binary firing vector of size $\sigma(\mathcal{E}_S) \times 1$	$u_{\psi, l}[k]$	Element of product firing matrix $\mathcal{U}[k]$
$U^+[k]$	Binary input firing vector of size $\sigma(\mathcal{E}_S) \times 1$		
$U^-[k]$	Binary output firing vector of size $\sigma(\mathcal{E}_S) \times 1$		
$u_\psi[k]$	Elements in the firing vector at associated times $t_k$		

**Word count: 6846**

## 1. Introduction

Industrial facilities are devoting ever greater attention to the importance of energy in their operations [1]. In some cases, industrial processes are energy intensive [2]. In other cases, such as with electric drives and motors, the energy supply must be of a very high quality [3]. Finally, many industrial companies are increasingly concerned with decarbonization either as imposed by regulation [4, 5], or stimulated by corporate social responsibility [6, 7]. To that end, onsite distributed renewable energy are often integrated. The combined objectives of high availability, quality and sustainability are often beyond the capabilities of the local utility and so this work considers *microgrid-enabled production systems* where the production enterprise has decided to in-source its energy supply so as to tailor its management and delivery to the needs of its production system. Microgrids have the potential to reduce local costs, energy losses, and greenhouse gases while enhancing energy reliability [8–10]. They also give owners the necessary autonomy to operate islanded from the local electric utility.

The introduction of microgrids to a production system setting opens several new industrial energy management activities in both planning and operations [11]. Energy planning focuses on energy efficiency. This static energy management approach optimizes the production system before it has been built, or when new technologies are incorporated in upgrades and retrofits [12, 13]. This not only considers production system resources, but also power systems resources, such as a microgrid infrastructure or the integration of renewable energy. Operations, or dynamic energy management, tries to optimize the usage of a given set of resources for energy consumption or cost [14, 15]. Such decisions coincide with the dynamics of the production system and may respond to several externalities, such as changes in the power grid balance, customer demand, and time-of-use prices [16–19].

Dynamic energy management is of particular importance to microgrid power balancing activities [20–24]. The trend of increasing renewable energy resources penetration in the power grid causes increases in variability and stochasticity of the power supply [25, 26]. Meanwhile, dynamic energy management controls the loads and has the potential to be a part of demand response [27, 28]. Furthermore, when operating in islanded model, the size of the microgrid limits the number of levers that control the balance; especially when the generation is stochastic. As a result, the production system and microgrid dynamics are coupled and cannot be studied separately. Energy consumption is a *byproduct* of production system activities, and the added value of energy differs per activity [29–31]. Consequently, online approaches that rely on multi-agent structures, or reactive control [32] have been developed. Meanwhile offline approaches, based on resource constraint scheduling methods or weighted multi-objective optimization have been discussed extensively [33, 34].

However, these studies do not include multi-discipline models, where the production system and microgrid dynamics are described in an unambiguous language. The need for such a multi-layer model has been discussed extensively by the network sciences community. An important remark made in [35] is that hetero-functional multi-layer models capture the interdependency and interaction of systems in a way that two separate mono-layer models cannot comprehend. This comprehension is essential to understanding structural properties such as resilience, robustness, and

centrality. The approach presented in this work has been already used to study the resilience of hetero-functional networks [36].

### 1.1. Scope

In developing a dynamic model for the energy management of microgrid-enabled production systems, the work restricts scope to discrete-part production systems. It also allows the microgrid to have a significant penetration of variable (renewable) energy resources. To ground the discussion, it is useful to consider a bird feeder manufacturing system [37–39] which is detailed later in Section 4 as an illustrative example.

Table 1: Microgrid-Enabled Production System Operations Management Decisions

<b>Product Dispatch</b>	When a given product part should undergo production in the facility.
<b>Integrated Planning &amp; Scheduling</b>	Which sequence of processes should be used to create the product.
<b>W.I.P. Management</b>	When & where the product parts should be buffered.
<b>Peak Load Management</b>	At a given machine, when the product parts should be processed to meet the production schedule and power grid constraints.
<b>Ancillary Services</b>	Given the dynamics of the power grid, how can the planning & scheduling of production activities support stabilization.

The dynamic model for microgrid-enabled production systems must also be able to accommodate several operations management decisions. Such decisions, when made, serve to advance the physical state and outputs of the microgrid-enabled production system so as to achieve its operations management objectives. These are summarized in Table 1. The first decision is dispatch of product parts to different machines to undergo transforming (value-adding) processes. Second, planning and schedule determines the sequence and timing of production processes as the product parts advance through the facility. Third, it is important to actively manage where and if work-in-progress will be buffered. These three decisions are inherently coupled to the microgrid power balance. They must now also simultaneously manage the peak load constraints of the microgrid. Finally, it is possible that the operations management decisions of the production system can serve to provide ancillary services that stabilize the microgrid.

### 1.2. Contribution

This paper seeks to develop a dynamic model for the energy management of microgrid-enabled production systems. The goal of the model is to simultaneously analyze the flows of products in a discrete-part production system and the power flows in the coupled microgrid. The model is developed in such a way as to describe a production system and microgrid of arbitrary size, topology and coupling. The model also specifically includes renewable energy to support the objective of greater sustainability. The load balance requirements resulting from the renewable energy integration impose the need for a dispatchable generator, with related carbon emissions.

58 Meanwhile, this work advances a broader body of literature in the network sciences called *multi-layer networks*  
 59 [35]. Very few works present models where the layers do not have to be aligned or of the same size. The work  
 60 presented in this paper advances the theory of multi-layer networks, as a result of the aforementioned coupling of the  
 61 production system and the microgrid.

62 The model developed here is based on a *hetero-functional graph theory* rooted in the Axiomatic Design for Large  
 63 Flexible Engineering Systems[40, 41]. The approach has been used to develop measures of reconfigurability of  
 64 production systems [37–39, 42]. Later it was applied to model other complex multi-layer systems such as the trans-  
 65 portation [43–46], water [47], and power domains [48]. Several recent works also demonstrate how the theory may  
 66 be applied to decision-marking; including the development of Multi-Agent System Design principles for both Future  
 67 Power Systems [48] and Reconfigurable Mechatronic Systems [49].

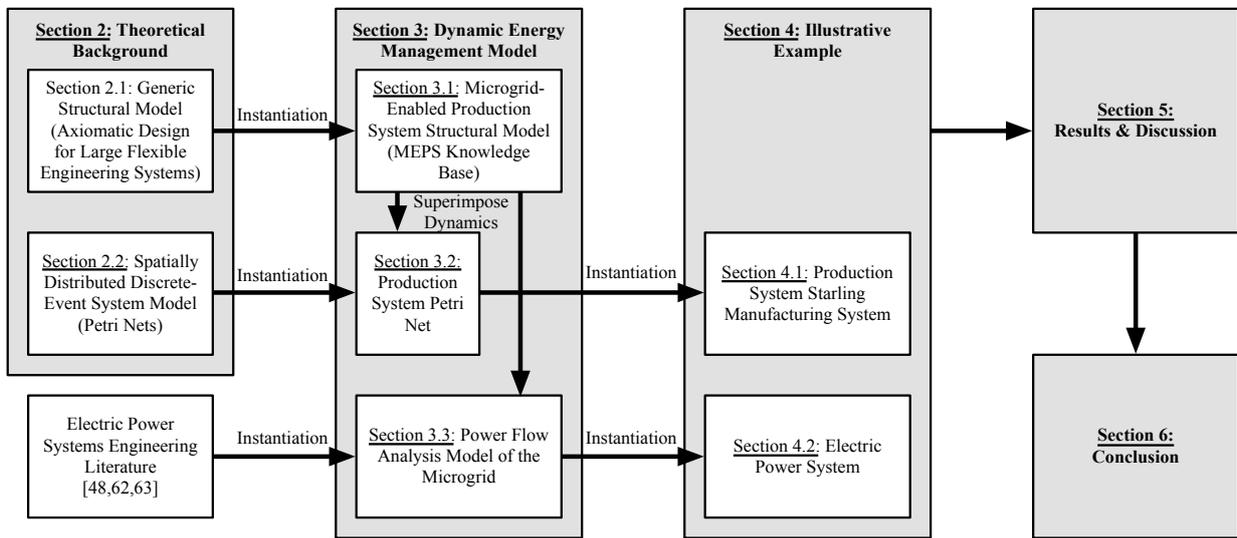


Figure 1: Visual representation of the document structure. Section numbers in top right.

68 Figure 1 provides an overview of the logical flow of the paper. The block elements are numbered consistently with  
 69 their associated section numbers. Section 2 lays the methodological foundation of hetero-functional graph theory.  
 70 Section 2.1 utilizes Axiomatic Design for Large Flexible Engineering Systems (AD4LFES) as generic model of  
 71 system structure and Section 2.2 uses Petri nets as a generic model of spatially distributed discrete-event dynamics.  
 72 Section 3 then develops the dynamic model for energy management by instantiation. Section 3.1 uses AD4LFES to  
 73 develop a structural model of a microgrid-enabled production system. Section 3.2 and Section 3.3 then superimpose  
 74 dynamics upon this structure to develop a production system petri net model and a power flow analysis model of the  
 75 microgrid respectively. Section 4 introduces a case study consisting of an example production system connected to  
 76 an example microgrid electric power system. Section 5 then presents and discusses the results of the case study as a  
 77 validation of the model. The article is concluded with Section 6.

## 2. Background

The methodological foundation of this work is a hetero-functional graph theory rooted in Axiomatic Design for Large Flexible Engineering Systems and Petri nets. The former is a concise way of describing the system structure and is discussed in subsection 2.1. The latter describes the system behavior as discrete-event dynamics. It is discussed in subsection 2.2.

### 2.1. Axiomatic Design for Large Flexible Engineering Systems

Microgrid-enabled production systems may be classified as a Large Flexible Engineering System. This subsection recalls how Axiomatic Design treats these systems in terms of their system resources, system processes, and the allocation of the latter to the former [42, 44–50]

**Definition 1. Large Flexible Engineering System (LFES)** [36, 51]: an engineering system with many functional requirements that not only evolve over time, but also can be fulfilled by one or more design parameters.

Although this paper relies on an Axiomatic Design structural model, it departs from its terminology without any change in interpretation. The functional requirements and the design parameters are understood to be mutually exclusive and collectively exhaustive sets of the system's processes (P) and resources (R). As a theory, Axiomatic Design presents several advantages that are directly relevant to microgrid-enabled production systems.

These include modeling support for:

- systems of heterogeneous modes of production (but identical function)
- systems of a fundamentally hetero-functional nature.
- the allocation of system function to form.
- systems of variable structure to support reconfigurable operation.

The set of system's resources  $R = M \cup B \cup H$  are classified as the set transforming resources  $M = \{m_1, \dots, m_{\sigma(M)}\}$ , independent buffers  $B = \{b_1, \dots, b_{\sigma(B)}\}$ , and transporting resources  $H = \{h_1, \dots, h_{\sigma(H)}\}$ , with  $\sigma()$  being the size of the set. For later simplicity, the set of buffers  $B_S = M \cup B$  is also defined [42, 50]. Since Axiomatic Design for LFES supports modelling of complex systems, aggregating of resources  $R$  can be useful to combine different systems. The aggregation matrix  $\mathcal{A}$  assigns resource  $r_j$  to aggregated resource  $r_i$  to create the set of aggregated resources  $\underline{R}$  [38, 39].

$$\underline{R} = \mathcal{A} \otimes R \quad (1)$$

**Definition 2. Aggregation Operator  $\otimes$**  [38, 39]: Given boolean matrix  $A$  and sets  $B$  and  $C$ ,  $C = A \otimes B$  is equivalent to:

$$C(i) = \bigcup_j a(i, j) \wedge b(j) \quad (2)$$

106 The set of system's processes  $P$  can be classified as the set of transforming, transporting, and holding processes.

107 **Definition 3. Transformation Process**[39, 42, 50]: A resource-independent, technology-independent process  $p_{\mu_j} \in$   
 108  $P_{\mu} = \{p_{\mu_1} \dots p_{\mu_{\sigma(P_{\mu})}}\}$  that transforms an artifact from one form into another.

109 **Definition 4. Transportation Process** [39, 42, 50]: A resource-independent process  $p_{\eta u} \in P_{\eta} = \{p_{\eta_1} \dots p_{\eta_{\sigma(P_{\eta})}}\}$  that  
 110 transports artifacts from one buffer  $b_{sy_1}$  to  $b_{sy_2}$ . There are  $\sigma^2(B_S)$  such processes of which  $\sigma(B_S)$  are "null" processes  
 111 where no motion occurs. The following convention of indices is adopted:

$$u = \sigma(B_S)(y_1 - 1) + y_2 \quad (3)$$

112 This convention implies a directed bipartite graph between the set of independent buffers and the transportation  
 113 processes whose incidence out  $M_H^-$  and incidence in  $M_H^+$  matrices are given by [48]:

$$M_H^- = \sum_{y1=1}^{\sigma(B_S)} e_{y1}^{\sigma(B_S)} [e_{y1}^{\sigma(B_S)} \otimes \mathbf{1}^{\sigma(B_S)}]^T \quad (4)$$

$$M_H^+ = \sum_{y2=1}^{\sigma(B_S)} e_{y2}^{\sigma(B_S)} [\mathbf{1}^{\sigma(B_S)} \otimes e_{y2}^{\sigma(B_S)}]^T \quad (5)$$

114 where  $\mathbf{1}^n$  is a column ones vector of predefined length  $n$ ,  $e_i^n$  is the  $i^{\text{th}}$  elementary basis vector, and  $\otimes$  is the kronecker  
 115 product.

117 **Definition 5. Holding Process** [39, 42, 50]: A transportation independent process  $p_{\varphi g} \in P_{\varphi}$  that holds artifacts during  
 118 the transportation from one buffer to another.

119 Together, the system processes and resources address hetero-functionality in a LFES.

120 System processes  $P$  are allocated to system resources  $R$  via the system knowledge base  $J_S$ . The Axiomatic Design  
 121 equation describes the allocation [39, 42, 50]:

$$P = J_S \odot R \quad (6)$$

122 where  $\odot$  is matrix boolean multiplication and  $J_S$  is defined as:

123 **Definition 6. System Knowledge Base** [39, 42, 50]: A binary matrix  $J_S$  of size  $\sigma(P) \times \sigma(R)$  whose element  $J_S(w, v) \in$   
 124  $\{0, 1\}$  is equal to one when action  $e_{wv}$  (in the SysML sense [52]) exists as a system process  $p_w \in P$  being executed by  
 125 a resource  $r_v \in R$ .

The system knowledge base  $J_S$  is constructed based on the smaller knowledge bases that address transformation, transportation and holding processes individually.

$$\begin{aligned} P_{\mu} &= J_M \odot M \\ P_{\eta} &= J_H \odot R \\ P_{\varphi} &= J_{\varphi} \odot R \end{aligned} \quad (7)$$

126  $J_S$  then becomes [39, 42, 50]:

$$J_S = \left[ \begin{array}{c|c} J_M & \mathbf{0} \\ \hline & J_{\bar{H}} \end{array} \right] \quad (8)$$

127 where in order to account for the simultaneity of holding and transportation processes into refined transportation  
128 processes  $P_{\bar{H}}$  [39, 42, 50]:

$$J_{\bar{H}} = [J_{\varphi} \otimes \mathbb{1}^{\sigma(P_{\eta})}] \cdot [\mathbb{1}^{\sigma(P_{\varphi})} \otimes J_H] \quad (9)$$

129 where  $\cdot$  is the hadamard product.

130 The system knowledge base has an additional property in that it defines the LFES structural degrees of freedom.  
131 These are important in the construction of the dynamic system state vector in large complex systems.

132 **Definition 7. Structural Degrees of Freedom** [39, 42, 50]: The set of independent actions  $\psi_i \in \mathcal{E}_S$  that completely  
133 defines the available processes in a LFES. Their number is given by:

$$DOF_S = \sigma(\mathcal{E}_S) = \sum_w^{\sigma(P)} \sum_v^{\sigma(R)} J_S(w, v) \ominus K_S(w, v) \quad (10)$$

134 where  $\ominus$  is boolean subtraction and  $K_S$  is a constraints matrix of appropriate size that eliminates actions from the  
135 action set. It serves to distinguish between the existence and the availability of a degree of freedom. For example,  
136 scheduled maintenance can disable a degree of freedom removing it from the system structure.

137 Previous work has applied a vectorization of the system knowledge base for mathematical convenience [48]. The  
138 shorthand  $()^V$  is used to replace  $vec()$ . Additionally, a projection operator projects the vectorized knowledge base onto  
139 a one's vector to eliminate sparsity  $\mathbb{P}J_S^V = \mathbb{1}^{\sigma(\mathcal{E}_S)}$ . While solutions for  $\mathbb{P}$  are not unique, this work chooses:

$$\mathbb{P} = \left[ e_{\psi_1}^{\sigma(P)\sigma(R)}, \dots, e_{\psi_{\sigma(\mathcal{E}_S)}}^{\sigma(P)\sigma(R)} \right] \quad (11)$$

140 where  $e_{\psi_i}^{\sigma(P)\sigma(R)}$  is the  $\psi_i^{th}$  elementary row vector corresponding to the first up to the last structural degree of freedom  
141 in increasing order.

## 142 2.2. Petri Nets

143 Petri nets are a concise and commonly used tool to model discrete part production system dynamics. This subsection  
144 describes their untimed and timed variants for later use.

145 **Definition 8. Marked Petri Net (Graph)**[53]: A bipartite directed graph represented as a 5-tuple  $\mathcal{N} = \{B_S, \mathcal{E}_S, \mathcal{M}, W, Q_B\}$   
146 where:

- 147 •  $B_S$  is a finite set of places of size  $\sigma(B_S)$ .
- 148 •  $\mathcal{E}_S$  is a finite set of transitions/events of size  $\sigma(\mathcal{E}_S)$ .
- 149 •  $\mathcal{M}_{PN} \subseteq (B_S \times \mathcal{E}_S) \cup (\mathcal{E}_S \times B_S)$  is a set of arcs of size  $\sigma(\mathcal{M}_{PN})$  from places to transitions and from transitions to  
150 places in the graph.

- 151 •  $W : \mathcal{M}_{PN} \rightarrow \{0, 1\}$  is the weighting function on arcs.
- 152 •  $Q_B$  is a marking (or discrete state) vector of size  $\sigma(B_S) \times 1 \in \mathbb{N}^{\sigma(B_S)}$ .

153 The arcs of the Petri net graph and its weightings define the Petri net incidence matrix.

154 **Definition 9. Petri Net Incidence Matrix**[53]: An incidence matrix  $\mathcal{M}$  of size  $\sigma(B_S) \times \sigma(\mathcal{E}_S)$  where:

$$\mathcal{M} = \mathcal{M}^+ - \mathcal{M}^- \quad (12)$$

155 where  $\mathcal{M}^+(y, \psi) = w(e_{wv}, b_y)$  and  $\mathcal{M}^-(y, \psi) = w(b_y, e_{wv})$  and  $\psi$  is a unique index mapped from the ordered pair  $(w, v)$ .

156 The Petri-net structure leads directly to the definition of its discrete-event dynamics.

157 **Definition 10. Petri Net (Discrete-Event) Dynamics**[53]: Given a binary firing vector  $U[k]$  of size  $\sigma(\mathcal{E}_S) \times 1$  and  
 158 a Petri-net incidence matrix  $\mathcal{M}$  of size  $\sigma(B_S) \times \sigma(\mathcal{E}_S)$ , the evolution of the marking vector  $Q_B$  is given by the state  
 159 transition function  $\Phi(Q_B[k], U[k])$ :

$$Q_B[k + 1] = \Phi(Q_B, U[k]) = Q_B[k] + \mathcal{M}U[k] \quad (13)$$

160 Beyond ordinary Petri nets, timed Petri as their name suggests introduce time into the dynamics definition

161 **Definition 11. Timed Petri Net (Discrete-Event) Dynamics**[54]: Given a binary input firing vector  $U^+[k]$  and a  
 162 binary output firing vector  $U^-[k]$  both of size  $\sigma(\mathcal{E}_S) \times 1$ , and the positive and negative components  $\mathcal{M}^+$  and  $\mathcal{M}^-$  of the  
 163 Petri-net incidence matrix of size  $\sigma(B_S) \times \sigma(\mathcal{E}_S)$ , the evolution of the marking vector  $Q$  is given by the state transition  
 164 function  $\Phi_T(Q[k], U^-[k], U^+[k])$ :

$$Q[k + 1] = \Phi_T(Q[k], U^-[k], U^+[k]) \quad (14)$$

where  $Q = [Q_B; Q_E]$  and

$$Q_B[k + 1] = Q_B[k] + \mathcal{M}^+U^+[k] - \mathcal{M}^-U^-[k] \quad (15)$$

$$Q_E[k + 1] = Q_E[k] - U^+[k] + U^-[k] \quad (16)$$

165 Note that Timed Petri Nets separate the infinitesimally short firing vector of ordinary Petri nets into distinct input and  
 166 the output firing vectors separated by processing times.  $Q_B$  and  $Q_E$  track the location of the tokens in the production  
 167 system.  $Q_B$  tracks the states of the buffers and  $Q_E$  the state of (ongoing) transitions [54, 55]. The transitions are fired  
 168 based on a scheduled event list that combines the discrete events with a time interval.

169 **Definition 12. Scheduled Event List**[53]: A tuple  $\mathcal{S} = (u_\psi[k], t_k)$  consisting of all elements  $u_\psi[k]$  in firing vectors  
 170  $U^-[k]$  and their associated times  $t_k$ . For every element,  $u_\psi^-[k] \in U^-[k]$ , there exists another element  $u_\psi^+[k] \in U^+[k]$   
 171 which occurs at time  $t_k + d_\psi$  time units later.  $t_k = t_k + d_\psi$ .

Table 2: System Processes &amp; Resources in a microgrid-enabled production system[38, 39, 56]

	$P_\mu$	$P_\eta$	$P_\varphi$	$M$	$B$	$H$	$J_S$
<b>LFES</b>	Transformation	Transportation	Holding	Transforming Resource	Independent Buffer	Transportation Resource	Knowledge Base
<b>Production System</b>	Transformation ( $P_{\mu PS}$ )	Transportation ( $P_{\eta PS}$ )	Holding ( $P_{\varphi PS}$ )	Machines ( $M_{PS}$ )	Input & Output Buffers ( $B_{PS}$ )	Material Handlers ( $H_{PS}$ )	Production System Knowledge Base ( $J_{PS}$ )
<b>Microgrid</b>	Generation & Consumption ( $P_{\mu MG}$ )	Transmission ( $P_{\eta MG}$ )	Voltage Level ( $P_{\varphi MG}$ )	Generators & Loads ( $M_{MG}$ )	Substations & Storage ( $B_{MG}$ )	Lines ( $H_{MG}$ )	Microgrid Knowledge Base ( $J_{MG}$ )

### 3. Model Development

This section develops the Dynamic Energy Management Model for Microgrid-Enabled Production Systems using Axiomatic Design, timed Petri-nets and physical modeling. First, a single knowledge base for the microgrid-enabled production system is constructed as a succinct description of system structure. The remainder of the section addresses the system behavior using the Axiomatic Design knowledge base as a foundation. A timed Petri-net model is derived to describe the production system's discrete event dynamics. Finally, a power flow analysis model is added as a physical model of the microgrid that allows for energy management by analyzing the system behavior [57]. The development represents a logical extension of the production system model in [58] and the transportation electrification model in [43, 45].

#### 3.1. Microgrid-Enabled Production System Knowledge Base

This subsection constructs the Microgrid-Enabled Production System Knowledge Base as an overlapping union of two underlying knowledge bases; one for the production system and the other for the microgrid. Table 2 provides an overview of the definitions of the resources and processes for each of these systems.

##### 3.1.1. Production System Knowledge Base

The production system knowledge base  $J_{PS}$  is constructed based on the concepts discussed in Section 2.1. First, the production system resources  $R_{PS}$  are defined as; the transformation resources  $M_{PS}$  that represent the transforming (value-adding) machines in the production system, the independent buffers  $B_{PS}$  that represent the input, output, and intermediate buffers, and the transportation resources  $H_{PS}$  that represent the material handlers that relocate product parts [39, 42, 58]. The set of all buffers is also defined as  $B_{S_{PS}} = M_{PS} \cup B_{PS}$ . Additionally, Definitions 3, 4, and 5 are followed to define the production system's transformation  $P_{\mu PS}$ , transportation  $P_{\eta PS}$ , and holding processes  $P_{\varphi PS}$ , resulting in the set of production system processes:  $P_{PS} = P_{\mu PS} \cup P_{\eta PS} \cup P_{\varphi PS}$ . Finally, the production system processes are mapped on the production system resources [39, 42, 58]. The system knowledge base consists of a

194 combination of the underlying knowledge bases, using Equation 6, 8 and 9.

$$J_{PS} = \left[ \begin{array}{c|c} J_{M_{PS}} & \mathbf{0} \\ \hline & J_{\bar{H}_{PS}} \end{array} \right] \quad (17)$$

195 where

$$J_{\bar{H}_{PS}} = \left[ J_{\varphi_{PS}} \otimes \mathbf{1}^{\sigma(P_{\eta_{PS}})} \right] \cdot \left[ \mathbf{1}^{\sigma(P_{\varphi_{PS}})} \otimes J_{H_{PS}} \right] \quad (18)$$

196

### 197 3.1.2. Microgrid Knowledge Base

198 The power system knowledge base is constructed similarly. First, the power system resources are defined. The  
 199 transformation resources  $M_{MG}$  include the systems generators and loads. The independent buffers  $B_{MG}$  represent  
 200 buffering capacity in the system, such as energy storage (e.g. batteries) or buses. Substations are modeled as inde-  
 201 pendent buffers without storage capacity. The transportation resources  $H_{MG}$  represent the power lines between the  
 202 buses, generators, and loads [48]. Next, Definitions 3, 4, and 5 are applied to define the microgrid's system pro-  
 203 cesses. The transformation processes  $P_{\mu_{MG}}$  represent the generation and consumption of power. The transportation  
 204 processes  $P_{\eta_{MG}}$  represent the power flow through the system. The holding processes  $P_{\varphi_{MG}}$  represent different voltage  
 205 levels as different ways of “carrying” power. These types of processes are combined in the set of microgrid processes  
 206  $P_{MG} = P_{\mu_{MG}} \cup P_{\eta_{MG}} \cup P_{\varphi_{MG}}$ . Finally, the microgrid system processes are mapped on to its resources [48]. The system  
 207 knowledge base consists of a combination of the underlying knowledge bases, using Equation 6, 8 and 9.

$$J_{MG} = \left[ \begin{array}{c|c} J_{M_{MG}} & \mathbf{0} \\ \hline & J_{\bar{H}_{MG}} \end{array} \right] \quad (19)$$

208 where  $J_{\bar{H}_{MG}} = J_{H_{MG}}$  is assumed, given that microgrids usually only retain one voltage level. Note that every trans-  
 209 portation resource (power line) is related to two transportation processes, one for each direction. Also note that the  
 210 transforming resources can realize either power generation or a consumption process but not both.

### 211 3.1.3. Microgrid Enabled Production System Knowledge Base

212 The Microgrid-Enabled Production System knowledge base is a union of the two previously identified knowledge  
 213 bases  $J_{PS}$  and  $J_{MG}$ . However, the two systems are not mutually exclusive. The transformation resources in the power  
 214 system overlap with production system's resources. The resulting transformation resources for the Microgrid-Enabled  
 215 Production System ( $M_{MPS}$ ) can be defined as:  $M_{MPS} = R_{PS} \cup \tilde{M}_{MG} = M_{PS} \cup B_{PS} \cup H_{PS} \cup \tilde{M}_{MG}$  where  $\tilde{M}_{MG}$  is taken  
 216 as the set of generators, and loads unrelated to production. Similarly, the production system processes are combined  
 217 with the microgrid transformation processes:  $P_{\mu_{MPS}} = P_{PS} \cup \tilde{P}_{\mu_{MG}} = P_{\mu_{PS}} \cup P_{\eta_{PS}} \cup \tilde{P}_{\mu_{MG}}$  where  $\tilde{P}_{\mu_{MG}}$  is taken as  
 218 the set of generating and consuming processes unrelated to production. In order to relate these sets of processes and  
 219 resources, three mutually exclusive knowledge bases are introduced:  $J_{M_{MPS}}$ ,  $J_{\bar{H}_{MPS}}$ , and  $\tilde{J}_{M_{MG}}$  where:

$$\begin{aligned}
P_{\mu MPS} &= J_{MPS} \odot M_{PS} \\
P_{\bar{\eta}PS} &= J_{\bar{H}MPS} \odot R_{PS} \\
\tilde{P}_{\mu MG} &= \tilde{J}_{M_{MG}} \odot \tilde{M}_{MG}
\end{aligned} \tag{20}$$

220 similarly to as defined in Equation 7.

221 Consequently, the Microgrid-Enabled Production System knowledge base  $J_{MPS}$ , as a type of large flexible engi-  
222 neering system, takes on the structural form of Equation 8:

$$= \left[ \begin{array}{c|c} J_{MPS} & \mathbf{0} \\ \hline & J_{\bar{H}MPS} \end{array} \right] \tag{21}$$

Then substituting in Equation 17 gives:

$$= \left[ \begin{array}{c|c|c} J_{PS} & \mathbf{0} & \mathbf{0} \\ \hline \mathbf{0} & \tilde{J}_{M_{MG}} & \mathbf{0} \\ \hline & J_{\bar{H}MPS} & \end{array} \right] \tag{22}$$

A final decomposition by substitution of Equation 20 gives:

$$= \left[ \begin{array}{c|c|c|c} J_{MPS} & \mathbf{0} & \mathbf{0} & \mathbf{0} \\ \hline & J_{\bar{H}PS} & \mathbf{0} & \mathbf{0} \\ \hline \mathbf{0} & \mathbf{0} & \tilde{J}_{M_{MG}} & \mathbf{0} \\ \hline & J_{\bar{H}MPS} & & \end{array} \right] \tag{23}$$

223

### 224 3.2. Dynamics of the Production System Domain

225 This subsection uses Petri-nets to describe the discrete-event dynamics in the production system domain. Two  
226 types of Petri nets are constructed. The first is called the production system Petri net and describes the evolution of  
227 the system processes and resources of the production system as they were originally defined in the Axiomatic Design  
228 knowledge base. The second is called the product Petri net and describes the evolution of products as they evolve from  
229 raw goods into finished ones. Structurally, it is also built upon the Axiomatic Design knowledge base. Dynamically,  
230 it is synchronized with the evolution of the production system Petri net. It is worth mentioning, that at first glance, the  
231 developed Petri-nets resemble “resource-oriented Petri nets” in the literature [59]. While there are some similarities,  
232 a careful inspection reveals that the novel tie to Axiomatic Design assigns very different physical meanings to the  
233 Petri-net models. Those developed here have the added benefit of being graphically intuitive and can be validated to  
234 the axiomatic design knowledge base by inspection. The production system and product Petri nets are now discussed  
235 in turn.

236 3.2.1. Production System Petri Net

A discrete-part production system is governed by spatially-distributed discrete-event dynamics. Petri nets have been used extensively to model the behavior of production systems [53–55, 60, 61]. Here, a production system Petri net is defined as a timed Petri net according to Definitions 8 and 11. It is at this point that the production system knowledge base in Equation 17 is tied to the production system Petri net structure. The production system buffers  $B_S$  share notation with the production system Petri net places to emphasize their equivalence. Similarly, the Petri net transitions are equivalent to the structural degrees of freedom  $\mathcal{E}_S$ . Consequently, the Petri net incidence matrix in Definition 9 follows the convention in Equation 3. It may be calculated by Equation 12 where  $\mathcal{M}_{PS}^-$  and  $\mathcal{M}_{PS}^+$  are straightforwardly derived using Equations 4, 5 and 8.

$$\mathcal{M}_{PS}^- = \sum_{y1=1}^{\sigma(B_{SPS})} e_{y1}^{\sigma(B_{SPS})} \left[ \mathbb{P}(X_{y1}^-)^V \right]^T \quad (24)$$

where

$$X_{y1}^- = \left[ \begin{array}{c|c} \mathbb{1}^{\sigma(P_{\mu PS})} e_{y1}^{\sigma(B_{SPS})T} & \mathbf{0}^{\sigma(P_{\mu PS}) \times \sigma(R_H)} \\ \hline \mathbb{1}^{\sigma(P_{\varphi PS})} \otimes e_{y1}^{\sigma(B_{SPS})} & \otimes \mathbb{1}^{\sigma(R_{PS})T} \end{array} \right] \quad (25)$$

$$\mathcal{M}_{PS}^+ = \sum_{y2=1}^{\sigma(B_{SPS})} e_{y2}^{\sigma(B_{SPS})} \left[ \mathbb{P}(X_{y2}^+)^V \right]^T \quad (26)$$

where

$$X_{y2}^+ = \left[ \begin{array}{c|c} \mathbb{1}^{\sigma(P_{\mu PS})} e_{y2}^{\sigma(B_{SPS})T} & \mathbf{0}^{\sigma(P_{\mu PS}) \times \sigma(R_H)} \\ \hline \mathbb{1}^{\sigma(P_{\varphi PS})} \otimes \mathbb{1}^{\sigma(B_{SPS})} & \otimes e_{y2}^{\sigma(B_{SPS})} \quad \otimes \mathbb{1}^{\sigma(R_{PS})T} \end{array} \right] \quad (27)$$

To complete the production system Petri net model, capacity constraints can be applied. A capacity vector  $C_C$  of size  $\sigma(\mathcal{E}_S) \times 1 \in \mathbb{N}^{\sigma(\mathcal{E}_S)}$  limits the number of tokens within a given transition.

$$Q_{\mathcal{E}}[k] \leq C_C \quad \forall k \quad (28)$$

237 Each element of the input firing vectors is also constrained by the availability of the associated system resource and  
238 its capacity

$$u_{\psi}[k] \cdot [J_S(\omega, v) \ominus K_S(\omega, v)] < C_C(\psi) \quad (29)$$

239

240 3.2.2. Product Petri Net

241 In addition to the production system Petri net, a product Petri net is required to describe the evolution of products  
242 as each evolve from raw to finished state.

243 **Definition 13.** Product Petri Net [37–39, 58]: Given product  $l_i$ , a product net is a marked Petri net graph  $\mathcal{N}_{l_i} =$   
 244  $\{S_{l_i}, \mathcal{E}_{l_i}, \mathcal{M}_{l_i}, W_{l_i}, Q_{l_i}\}$  where:

- 245 •  $S_{l_i}$  is the set of product places that represents a product component at a raw, work-in-progress, or final stage of  
 246 production.
- 247 •  $\mathcal{E}_{l_i}$  is the set of product events that describe the transformation of the product between product places.
- 248 •  $\mathcal{M}_{l_i} \subseteq (S_{l_i} \times \mathcal{E}_{l_i}) \cup (\mathcal{E}_{l_i} \times S_{l_i})$  is the product arc relations that describe which products or components receive  
 249 which product events.
- 250 •  $W_{l_i} : \mathcal{M}_{l_i} \rightarrow \{0, 1\}$  is the weighting function on product arcs.
- 251 •  $Q_{l_i}$  is a marking vector that describes the product's evolution.

252 where

253 **Definition 14.** Product Event: A specific transformation process that may be applied to a given product.

254 and the associated (untimed) state transition function follows Definition 10.

$$Q_{l_i}[k + 1] = Q_{l_i}[k] + \mathcal{M}_{l_i} U_{l_i}[k] \quad (30)$$

255 where  $U_{l_i}[k]$  is the firing vector corresponding with product  $l_i$  at time  $k$ .

256 Note that a different product net is needed for each product type; each of which must be instantiated to support  
 257 each individual product on the shop floor. This supports mass-customized production and the intelligent product  
 258 paradigm. The interested reader is referred to the underlying references for detailed discussion [38, 56].

259 As expected, the production system Petri net and the product Petri net dynamics are inherently coupled. A product  
 260 firing matrix is introduced to synchronize the production system Petri net firing vectors with those of the product Petri  
 261 nets.

262 **Definition 15. Product Firing Matrix**[44, 45, 49]: a binary product firing matrix  $\mathcal{U}[k]$  of size  $\sigma(\mathcal{E}_S) \times \sigma(L)$  whose  
 263 element  $u_{\psi,l}[k] = 1$  when the  $k^{\text{th}}$  firing timing triggers a product  $l$  to take structural degree of freedom  $\psi$  for action.

264 Additionally, a product transformation feasibility matrix is required for each product to link product events to their  
 265 associated transformation processes in the production system.

266 **Definition 16. Product Transformation Feasibility Matrix**[37, 38, 49]: A binary matrix  $\Lambda_{\mu i}$  of size  $\sigma(\mathcal{E}_{l_i}) \times \sigma(P_{\mu})$   
 267 whose value  $\Lambda_{\mu i}(x, j) = 1$  iff  $\epsilon_{x l_i}$  realizes transformation process  $p_{\mu j}$ .

268 Consequently, the production system input firing vectors at a given moment  $k$  become [37, 38, 49]:

$$\Lambda_{\mu i}^T \cdot U_{l_i} = A_{i,j} \cdot \mathcal{U} \cdot e_{l_i}^{\sigma(L)T} \quad (31)$$

269 where  $e_i^n$  represents the  $i^{\text{th}}$  elementary basis vector of predefined length  $n$  and  $A_{i,j} = 1$  if  $p_{\mu i}$  is used in  $\epsilon_{S_j}$ .

### 270 3.3. Power Flow Analysis Model of the Microgrid

271 To complete the dynamic energy management model for a microgrid-enabled production system, a power flow  
 272 analysis model of the microgrid is introduced. To this end, the link between Axiomatic Design and power flow  
 273 analysis has been previously established [48] and is summarized here. Six steps are taken to establish the elements of  
 274 the power flow analysis.

275 The derivation of the power flow analysis model of the microgrid rests in the recognition that the production system  
 276 acts as a load on the microgrid and must be included. The first step specifies a device model for every structural degree  
 277 of freedom in  $J_{MPS}$ . In the device model, the set of algebraic state variables is defined as  $w_{E\psi} = [P_\psi, Q_\psi, v_\psi, \theta_\psi]$ , where

- 278 •  $P_\psi$  – is active power injection from ground.
- 279 •  $Q_\psi$  – is the associated reactive power injection from ground.
- 280 •  $v_\psi$  – is the associated voltage magnitude relative to ground.
- 281 •  $\theta_\psi$  – is the associated voltage angle relative to a predefined reference bus.

282 For each structural degree of freedom  $\psi$  [48], the device model for transportation structural degrees of freedom con-  
 283 tains a specific set of algebraic equations:

$$g_\psi = P_{E\psi} + jQ_\psi = (v_\psi \angle \theta_\psi) y_\psi^* (v_\psi \angle \theta_\psi)^* \quad (32)$$

284  
 285 In the second step, for convenience, the transportation degrees of freedom  $\mathcal{E}_{\psi H}$  are distinguished from the trans-  
 286 formation degrees of freedom  $\mathcal{E}_{\psi M}$ . Each element in the transportation structural degrees of freedom is also assigned  
 287 an admittance  $y_{\psi h}$ . These are organized into a transportation degree of freedom admittance matrix, which can be  
 288 compared with the line admittance matrix in traditional power flow analysis [48].

$$\mathcal{Y} = \text{diag}(y_{\psi h_1}, \dots, y_{\psi h_{\sigma(2H)}}) \quad (33)$$

289  
 290 The third step defines the transportation degree of freedom incidence matrix  $M_{\mathcal{E}_{\psi H}}$ , using Equations 4 and 5. The  
 291 transportation degree of freedom incidence matrix can be compared with the bus incidence matrix in traditional power  
 292 flow analysis [48].

$$M_{\mathcal{E}_{\psi H}} = M_{\mathcal{E}_{\psi H}}^+ - M_{\mathcal{E}_{\psi H}}^- \quad (34)$$

293 where

$$M_{\mathcal{E}_{\psi H}}^- = \sum_{y1=1}^{\sigma(Bs_{MPS})} e_{y1}^{\sigma(Bs_{MPS})} [P_H(X_{y1}^-) V] T \quad (35)$$

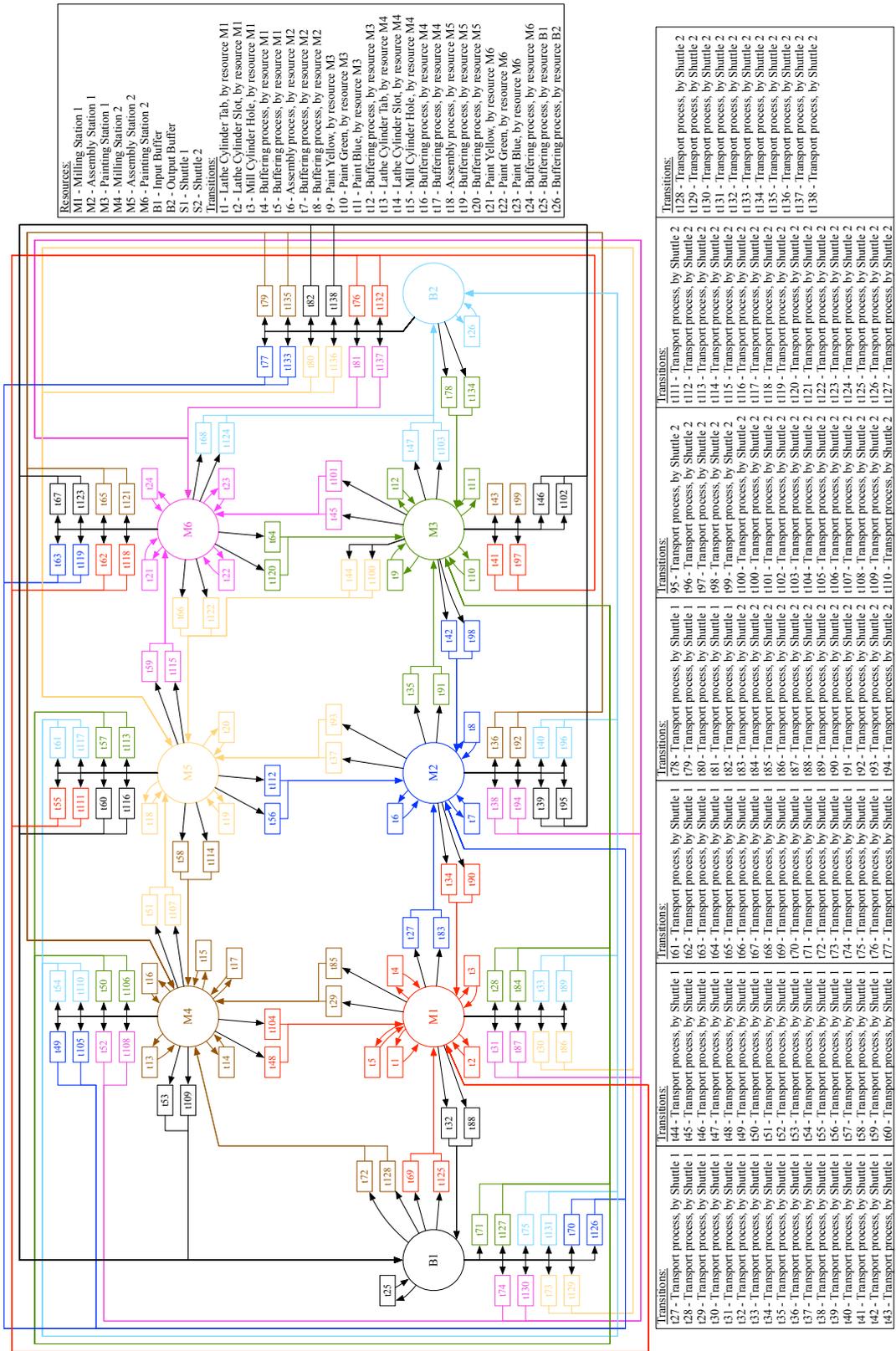


Figure 2: Petri Net Graph of the Starling Manufacturing System.

294 with:

$$X_{y_1}^- = e_{y_1}^{\sigma(B_{S_{MPS}})} \otimes \mathbb{1}^{\sigma(B_{S_{MPS}})} \otimes \mathbb{1}^{\sigma(R_{MPS})T} \quad (36)$$

295 and where

$$M_{\mathcal{E}_{\psi H}}^+ = \sum_{y_2=1}^{\sigma(B_{S_{MPS}})} e_{y_2}^{\sigma(B_{S_{MPS}})} [\mathbb{P}_H (X_{y_2}^+)^V]^T \quad (37)$$

296 with:

$$X_{y_2}^+ = \mathbb{1}^{\sigma(B_{S_{MPS}})} \otimes e_{y_2}^{\sigma(B_{S_{MPS}})} \otimes \mathbb{1}^{\sigma(R_{MPS})T} \quad (38)$$

297 and where

$$\mathbb{P}_H = [e_{\psi H_1}^{\sigma(P_\eta)\sigma(H)}, \dots, e_{\psi H_n}^{\sigma(P_\eta)\sigma(H)}] \quad (39)$$

298 The fourth step combines the transportation degrees of freedom admittance matrix (Equation 33) and incidence  
 299 matrix (Equation 34), to calculate the bus admittance matrix with size  $\sigma(B_{S_{MPS}}) \times \sigma(B_{S_{MPS}})$ , as traditionally defined  
 300 in power systems engineering [48, 62].

$$\mathbf{Y} = M_{\mathcal{E}_{\psi H}} * \mathcal{Y} * M_{\mathcal{E}_{\psi H}}^T \quad (40)$$

301

302 The fifth step extends the previously established derivation of the power flow analysis as the term  $\mathcal{M}$  is introduced  
 303 to allow for multiple degrees of freedom in one system resource [48].

$$M_E = \sum_{y_1=1}^{\sigma(B_S)} e_{y_1}^{\sigma(B_S)} [\mathbb{P}_M (\mathbb{1}^{\sigma(P_\mu)} e_{y_1}^{\sigma(M)})^V]^T \quad (41)$$

304 where

$$\mathbb{P}_M = [e_{\psi M_1}^{\sigma(P_\mu)\sigma(M)}, \dots, e_{\psi M_n}^{\sigma(P_\mu)\sigma(M)}] \quad (42)$$

305 As the final step, the power flow equations follow straightforwardly from Kirchoff's Current Law [48, 62, 63].

$$M_E [\mathbf{P}_E + j\mathbf{Q}] = \text{diag}(\mathbf{V}) \mathbf{Y}^* \mathbf{V}^* \quad (43)$$

306 where  $\mathbf{P}$ ,  $\mathbf{Q}$  are associated with transformation degrees of freedom.  $\mathbf{V}$  has size  $\sigma(B_{S_{MPS}}) \times \mathbf{1}$  and contains the nodal  
 307 voltage levels, as defined in the device model. In such a way, the relatively abstract Axiomatic Design knowledge  
 308 base is shown to be entirely consistent with traditional power flow analysis.

309 In conclusion, this section formulates a dynamic model for the energy management of microgrid-enabled produc-  
 310 tion systems. The model is dynamic in the sense that it represents the production system's discrete event dynamics  
 311 using Petri nets. It facilitates energy management in that the energy consumption of the production system is tightly  
 312 integrated with the underlying microgrid.

313 **4. Illustrative Example**

314 This section discusses an example for a Microgrid-Enabled Production System. This specific example is chosen  
 315 because it includes elements that cover all of the definitions in the microgrid-enabled production system model while  
 316 still retaining enough simplicity so as to give relatively intuitive results. The production system part of the system is  
 317 further detailed in Subsection 4.1. The microgrid part of the system is further detailed in Subsection 4.2.

318 *4.1. Production System*

319 The Starling Manufacturing System is a discrete part production system of bird feeders and depicted in Figure 3  
 320 [36, 37, 39]. It consists of ten resources; three pairs of transforming machines  $M_{PS} = \{\text{Machining Station 1, Assembly}$   
 321  $\text{Station 1, Painting Station 1, Machining Station 2, Assembly Station 2, Painting Station 2}\}$ , two independent buffers  
 322  $B_{PS} = \{\text{Input Buffer, Output Buffer}\}$ , and two transportation resources  $H_{PS} = \{\text{Shuttle A, Shuttle B}\}$ . The independent  
 323 buffers store product elements before and after processing in the production system. The transportation resources are  
 324 shuttles that move on tracks; following the direction of the arrows (as displayed in Figure 3).

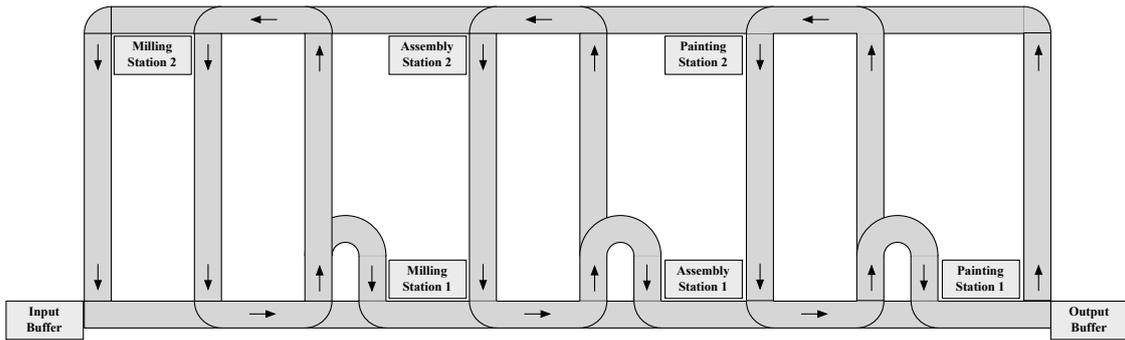


Figure 3: Starling Manufacturing System Overview

325 The bird feeders consist of three parts; a bottom, middle, and top cylinder. It is produced in seven transformation  
 326 processes  $P_{\mu PS} = \{\text{Lathe Tab, Lathe Slot, Mill Hole, Laminate, Paint Yellow, Paint Green, Paint Blue}\}$ . The transporta-  
 327 tion processes are  $P_{\eta PS} = \{m_i m_j, m_i b_k, b_k m_i, b_k b_l\} \forall i, j = 1, 2, 3, 4, 5, 6; k, l = 1, 2$  and move the product parts between  
 328 buffers. The holding processes account for three fixture configurations  $P_{\gamma PS} = \{\text{Small Radial, Big Radial, Axial}\}$ . The  
 329 allocation of the processes onto the resources using knowledge bases is demonstrated in earlier work.

330 Figure 2 on Page 17 shows the Petri net representation of the production system shown in Figure 3. Note that its  
 331 lay-out is similar to the physical production system lay-out. The Petri net contains places for the set of buffers  $B_S$ ,  
 332 that are oriented in a similar way as in Figure 3. Every process is related to one of the transitions. These represent the  
 333 production degrees of freedom. The incidence matrix is defined by Definition 9, or by inspection. The transitions are  
 334 fired based on a scheduled events list. This events list is imported from an external source and assumed to be constant.  
 335 The fired transitions are shown as a list in Table 3 on Page 20.

Table 3: Production System Firing Vectors [37]

Production System			Time		Product Net		
List Index (rows)	Transition	# Tokens Fired	T start	T end	Transition	# Tokens Fired	Name
1	25	7					Buffer
2	72	1	1	4			Transportation
3	125	1	1	4			Transportation
4	1	1	5	8	1	1	Lathe Cylinder Tab
5	13	1	5	8	4	1	Lathe Cylinder Tab
6	2	1	8	11	2	1	Lathe Cylinder Slot
7	14	1	8	11	5	1	Lathe Cylinder Slot
8	3	1	11	14	3	1	Mill Cylinder Hole
9	15	1	11	14	6	1	Mill Cylinder Hole
10	49	1	14	18			Transportation
11	83	1	14	18			Transportation
12	6	1	18	23	10	1	Assembly Process
13	72	1	18	22			Transportation
14	125	1	18	22			Transportation
15	1	1	22	25	7	1	Lathe Cylinder Tab
16	13	1	22	25	7	1	Lathe Cylinder Tab
17	7	1					Buffer
18	2	1	25	28	8	1	Lathe Cylinder Slot
19	14	1	25	28	8	1	Lathe Cylinder Slot
20	3	1	28	31	9	1	Mill Cylinder Hole
21	15	1	28	31	9	1	Mill Cylinder Hole
22	49	1	31	35			Transportation
23	83	1	31	35			Transportation
24	6	1	35	40	11	1	Assembly Process
25	7	1					Buffer
26	72	1	35	39			Transportation
27	125	1	35	39			Transportation
28	1	1	39	42	1	1	Lathe Cylinder Tab
29	13	1	39	42	4	1	Lathe Cylinder Tab
30	35	1	40	45			Transportation
31	2	1	42	45	2	1	Lathe Cylinder Slot
32	14	1	42	45	5	1	Lathe Cylinder Slot
33	3	1	45	48	3	1	Mill Cylinder Hole
34	9	1	45	51	12	1	Paint Yellow
35	15	1	45	48	6	1	Mill Cylinder Hole

Production System (cont'd)			Time (cont'd)		Product Net (cont'd)		
List Index (rows)	Transition	# Tokens Fired	T start	T end	Transition	# Tokens Fired	Name
36	49	1	48	52			Transportation
37	83	1	48	52			Transportation
38	12	1					Buffer
39	6	1	52	57	10	1	Assembly Process
40	72	1	52	56			Transportation
41	125	1	52	56			Transportation
42	1	1	56	59	1	1	Lathe Cylinder Tab
43	13	1	56	59	4	1	Lathe Cylinder Tab
44	47	1	56	60			Transportation
45	6	1	57	62	11	1	Assembly Process
46	2	1	59	62	2	1	Lathe Cylinder Slot
47	14	1	59	62	5	1	Lathe Cylinder Slot
48	26	1					Buffer
49	3	1	62	65	3	1	Mill Cylinder Hole
50	15	1	62	65	6	1	Mill Cylinder Hole
51	35	1	62	67			Transportation
52	4	1					Buffer
53	49	1	65	69			Transportation
54	10	1	67	73	12	1	Paint Green
55	83	1	67	73			Transportation
56	7	1					Buffer
57	72	1	69	73			Transportation
58	6	1	71	76	10	1	Assembly Process
59	13	1	73	76	7	1	Lathe Cylinder Tab
60	47	1	73	77			Transportation
61	7	1					Buffer
62	14	1	76	79	8	1	Lathe Cylinder Slot
63	26	1					Buffer
64	15	1	79	82	9	1	Mill Cylinder Hole
65	49	1	82	86			Transportation
66	6	1	86	91	11	1	Assembly Process
67	35	1	91	96			Transportation
68	11	1	96	102	12	1	Paint Blue
69	47	1	102	106			Transportation

336 The product net is based on the production sequence. The different stages are represented by places and the  
337 transformations equal transitions between product places. The product net for a yellow bird feeder is shown in Figure  
338 4. The product net dynamics are related to the firing vectors via the Production System Feasibility Matrix (Definition  
339 16). When a product part is neither processed nor buffered, it appears as a queue in the buffer state vector  $Q_S$ .  
340 However, all places have a transition that represents the buffering process. As a result, queues only occur when the  
341 capacity of the place is exceeded. The transition state vector  $Q_E$  shows the tokens per transition. The transitions  
342 consume a predefined amount of energy, which is added to the idling consumption of the machines. Additionally, the  
343 assumption is made that the transitions related to transportation resources and independent buffers do not consume  
344 power.

#### 345 4.2. Electric Power System

346 The microgrid lay-out is based on the microgrid in the book by Saadat [64]. The load buses are corresponding with  
347 the machines in the production system. The system consists of nine transforming or buffering resources  $B_{S_{MG}} = \{\text{Load}$

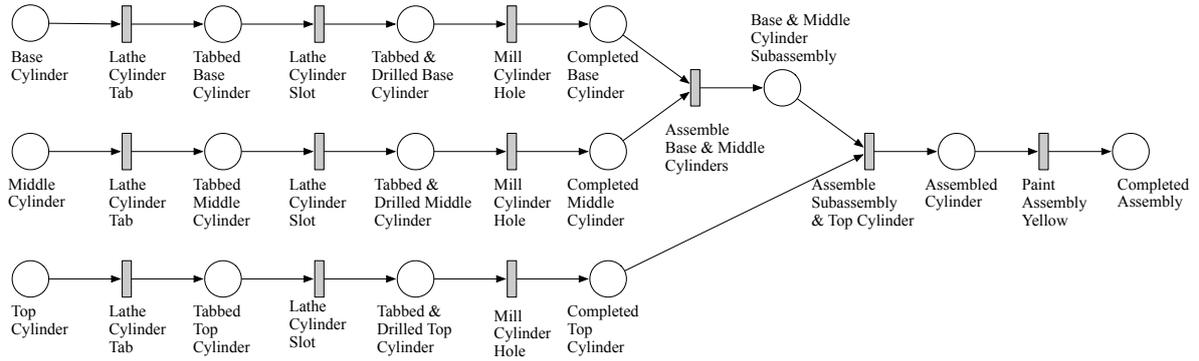


Figure 4: Product net for a yellow birdfeeder [37]

348 Bus 1, Load Bus 2, Load Bus 3, Load Bus 4, Load Bus 5, Load Bus 6, Slack Bus, RE Generator 1, RE Generator  
 349 2), where the Slack Bus is considered to be a dispatchable generator (i.e. a connection to the larger power grid, a  
 350 battery, etc). The transportation resources are the power lines  $H_{MG} = \{\text{Power Line 1}, \dots, \text{Power Line 10}\}$ . This set  
 351 of energy resources captures the breadth of functionality described in the Methodological Development (Section 3).  
 352 The transformation processes in the system are  $P_{\mu MG} = \{\text{Generate Power, Consume Power}\}$ . The holding processes  
 353  $P_{\varphi MG}$  are assumed to be the same for every bus and every power line and can thus be neglected. The transportation  
 354 processes  $P_{\eta MG}$  can be derived from Figure 5, in which the arrows leaving the buses indicate the loads.

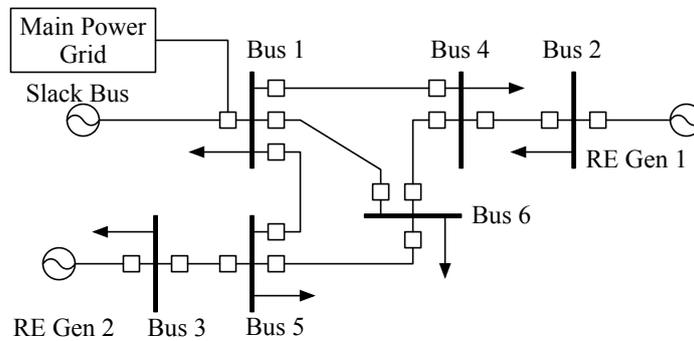


Figure 5: Overview of the Microgrid structure [64]

355 The input data for the renewable energy generators is generated by the DOE/NREL alliance [65]. The two re-  
 356 newable energy resources are assumed to be solar photovoltaics; each with a peak generation of 11.5 MW. Both the  
 357 power generation and the power consumption are assumed to contain solely the active power. Figure 7 shows the  
 358 energy generation curve of the generators independently and aggregated. The slack bus sustains the power balance in  
 359 the microgrid and is allowed to be both positive and negative. The slack bus can, for example, be a combination of a  
 360 connection with the power grid, to offload a generation surplus, and a gas turbine, to provide when there is a power

361 deficit. The gas turbine, in this illustrative example, is assumed to have a heat rate of 14,692.6 BTU/kWh at minimum  
 362 efficiency, and 11,302 BTU/kWh at maximum efficiency [66, 67].

363 This example demonstrated the breadth of function in the methodological development (Section 3). Future work  
 364 can add greater redundancy in both the production system as well as the power grid so as to more deeply investigate  
 365 control and optimization decision making algorithms.

## 366 5. Results & Discussion

367 The Microgrid-Enabled Production System model succeeds to integrate the microgrid and the production system  
 368 in one model. It aggregates both system resources and processes, which results in the shared knowledge base  $J_{MPS}$ .

369 The system transformation resources are  $M_{MPS} = \{\text{Machine 1, Machine 2, Machine 3, Machine 4, Machine 5,}$   
 370  $\text{Machine 6, Input Buffer, Output Buffer, Shuttle 1, Shuttle 2, Slack Bus, RE Generator 1, RE Generator 2}\}$ . The  
 371 system transportation resources are  $H_{MPS} = H_{MG}$ . The system transformation processes are  $P_{\mu MPS} = \{\text{Lathe Tab,}$   
 372  $\text{Lathe Slot, Mill Hole, Laminate, Paint Yellow, Paint Green, Paint Blue, } m_i m_j, m_i b_k, b_k m_i, b_k b_l, \text{ Generate Power}\}$   
 373  $\forall i, j = 1, 2, 3, 4, 5, 6; k, l = 1, 2$ . The system transportation processes  $P_{\eta MPS} = P_{\eta MG}$ .

374 Table 3 shows the transitions of the tokens in the product Petri net over time. By inspection it can be concluded  
 375 that the products evolve correctly through the product net.

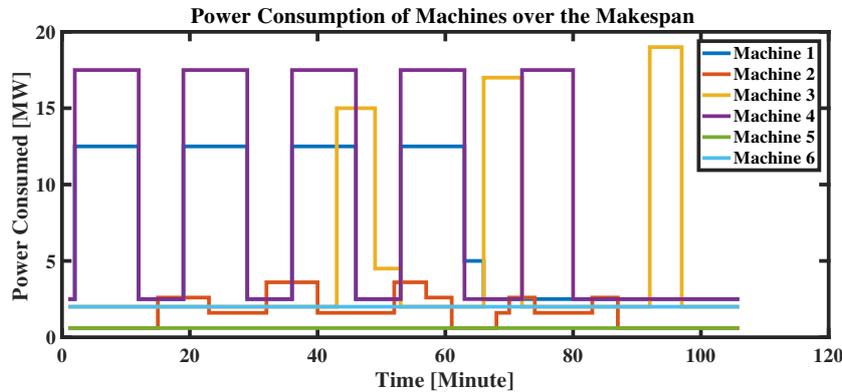


Figure 6: Energy Consumption of the Machines over Time

376 The transitions in the product net are coupled to the transitions in the production Petri net. Figure 6 shows  
 377 the energy consumption of the production system's machine over the duration of their production schedule of 110  
 378 minutes. The energy consumption of the machines is presented in Figure 6. This figure can be compared with the  
 379 product net transitions of Table 3 and by inspection the energy consumption of the machines corresponds with the  
 380 evolutions of the product parts. Additionally, the transitions have different levels of energy consumption in different  
 381 machines. This explains the difference in height between the curve of Machine 1 and Machine 4. Machine 5 and  
 382 Machine 6 consume a constant level of energy, which is the result of standing idle.

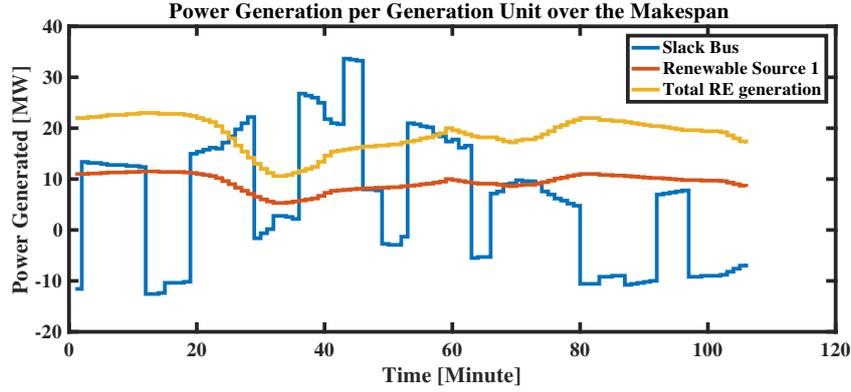


Figure 7: Energy Generation over Time

383 Figure 7 displays the energy generation of the three different energy sources over time. Two renewable energy  
 384 sources (solar photovoltaics) are included. These generators have the same pattern and the two lines represent the  
 385 individual pattern (RE. Gen. 1) and the aggregated pattern (RE. Gen. Total).

386 Both the renewable energy generation and the production system consumption are highly variable. The slack bus  
 387 needs to match the netload of the system. This clearly shows the challenge of islanded operation of a microgrid-  
 388 enabled production system, as the ramping speed of the slack bus needs to be large. To resolve this control problem,  
 389 there is a clear need to decrease the variability of the production system energy consumption.

390 Under the assumption that the gas turbine produces the power demand that is not provided by the renewable energy  
 391 resources, the CO<sub>2</sub> emissions can be calculated with the provided heat rate data. The heat rate decreases with more  
 392 efficient operation of the gas turbine and is thus modeled as a linear function of the relative load on the turbine. The  
 393 CO<sub>2</sub> emissions of the gas turbine are 53.07 Kilogram per 1 million BTU natural gas fed into the turbine. The CO<sub>2</sub> are  
 394 calculated as:

$$\text{CO}_2 \text{ emissions} = \left( \text{Carbon Intensity} \right) \left( \text{Heat Rate} \right) \left( \text{Electrical Energy} \right) \quad (44)$$

of Fuel [CO<sub>2</sub>/BTU] [BTU/MWh] Generated [MWh]

395 The resulting rate of CO<sub>2</sub> emissions is presented in Figure 8.

396 Generally speaking, the microgrid-enabled production system model shows that the production activities can  
 397 be directly coupled as a load to the microgrid. The two unlike systems come together in a model that addresses  
 398 the characteristics of each of the systems. The model shows that a production system that is optimized solely for  
 399 production, may impose an unwanted load on the microgrid. Consequently, grid balancing activities would need to  
 400 address this variable behavior; as demonstrated in Figure 7. The determination of the firing vectors can therefore  
 401 be viewed as an opportunity for decision-making that dynamically manages production activities with the energy  
 402 management of the microgrid. Finally, the model can be used to create a better insight in the detailed dynamics of the  
 403 microgrid (e.g. transient stability analysis) as has been demonstrated in [48].

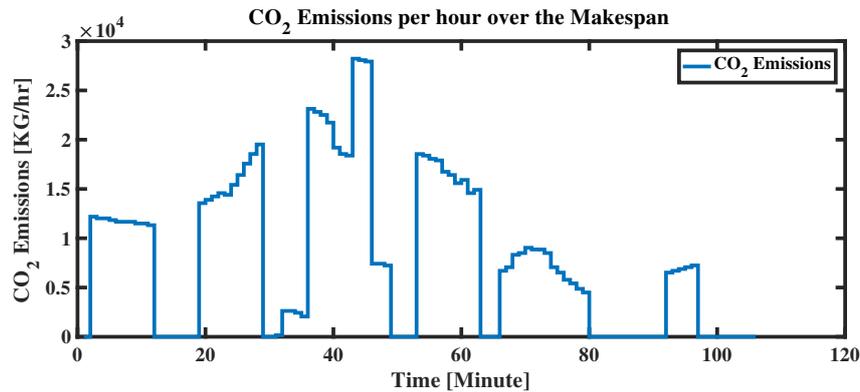


Figure 8: CO<sub>2</sub> emissions from the Gas Turbine over Time

## 404 6. Conclusion & Future Work

405 This article defines a dynamic model for the energy management of microgrid-enabled production systems. It  
 406 succeeds in integrating a production system model with a power grid model, using Axiomatic Design for Large Flex-  
 407 ible Engineering Systems. A mutually exclusive and collectively exhaustive description of processes and resources  
 408 is introduced, which form the basis of precise energy accounting and accurate grid operations. The power flow anal-  
 409 ysis analyzes the static state of the power system. The outcomes of the example show that the variable electricity  
 410 demand imposed by production activities is ill accommodated by the renewable energy sources alone. The slack bus  
 411 is necessary to maintain the balance on the microgrid. Additionally, this model can function to calculate requirements  
 412 for microgrid-enabled production facilities, more specifically energy storage and demand response. In future work,  
 413 this model may be used for energy management decisions using the firing vectors that control the production system  
 414 processes. Different system set ups can be compared on their electricity consumption and their microgrid impacts.

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